

7-9 Marks

Syllabus

Signal and System :-

- (i) Continuous signals (i) Introduction to the signals & system. (20 hrs)
- (ii) Continuous system (ii) LTI system. (8 hrs)
- (iii) CTFS (12 hrs)
- (iv) CTFT (18 hrs)
- (v) Laplace Transform (12-15 hrs)
- (vi) Sampling Theorem (3 hrs)
- (vii) Discrete signal and system.
- (viii) Z-Transform. (10 hrs)
- (ix) DTFT (6 hrs)
- (x) DFT & FFT (6 hrs)
- (xi) Digital Filters (4 hrs)
- (xii) Miscellaneous.

Electrical Engg.

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10/05/22

Chapter - 1

Introduction to the Signals & Systems

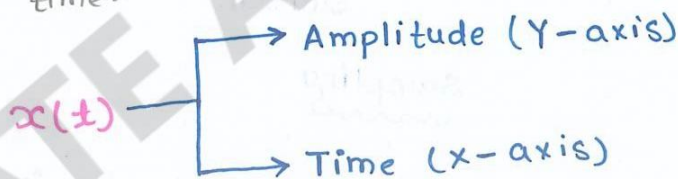
* What do you mean by Signal -

- Signal is an any indication about which some amount of information is convey to one place to other place.
- A signal is an any quantity having some information associated with it.
- It may also be defined as function of one or more independent variable which contains some information.

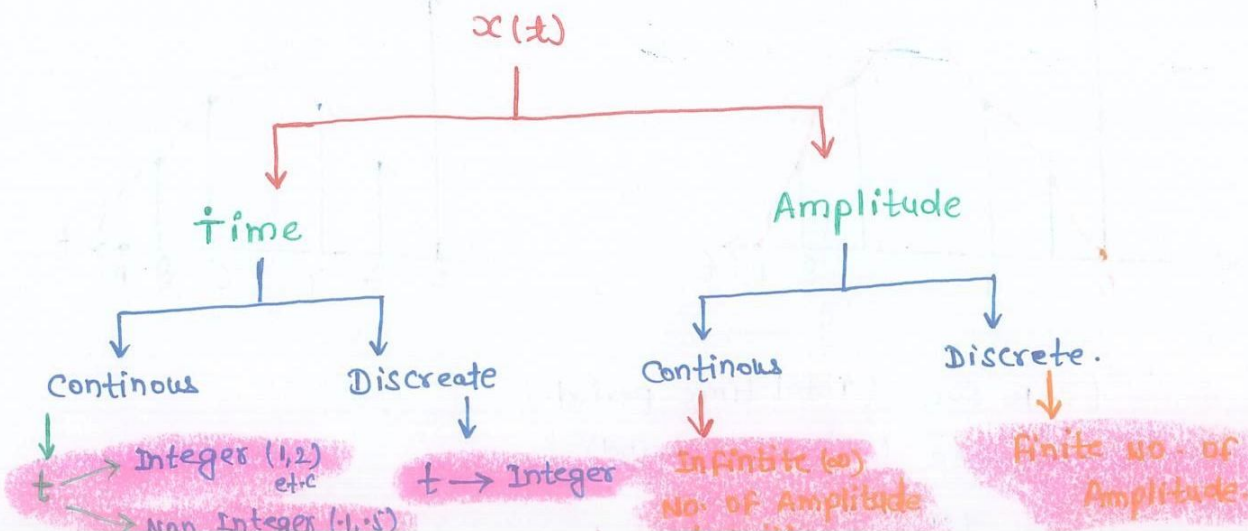
Example :- (i) A speech signal would be represented by acoustic pressure as a function of time.

(ii) A voltage signal defined as voltage across any element varying as a function of time.

Y-axis \rightarrow Amplitude
x-axis \rightarrow time



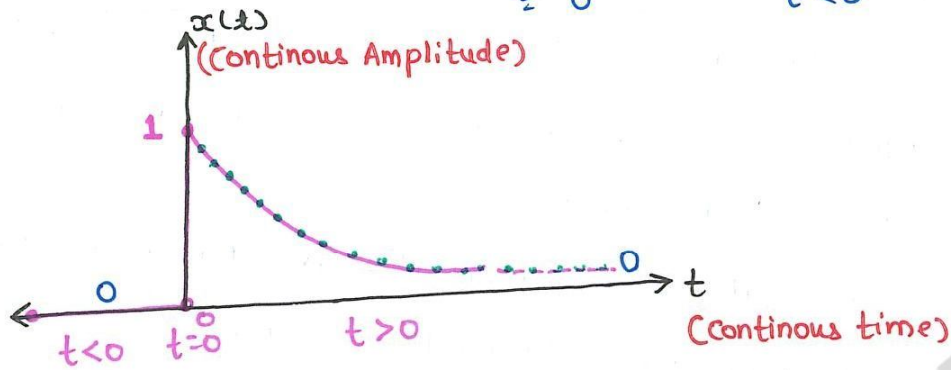
- Both Amplitude and Time can be continuous in time and also discrete with time.



i) Continuous Time & Continuous Amplitude Signal.

$$x(t) = e^{-2t} \cdot u(t) = e^{-2t} \cdot 1 \quad t \geq 0$$

$$= 0 \quad t < 0$$



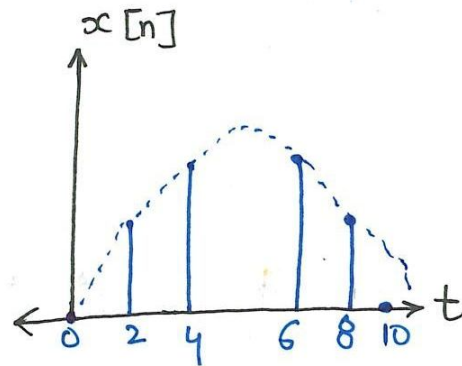
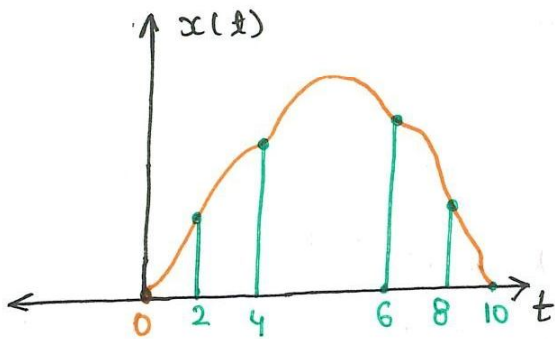
$$t=0 \Rightarrow \text{Amplitude} = e^0 = 1$$

$$t=\infty \Rightarrow \text{Amplitude} = e^{-\infty} = 0$$

Sampling :-



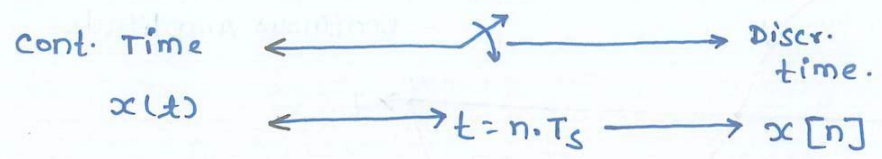
- The timing of switch OFF to ON is called sampling period.



$t = 10$ sec (Total time period)
 $T_s = 2$ sec (Sampling period)
 $n = 5$ (No. of samples)

$$t = n \cdot T_s$$

$$\frac{1}{T_s} = f_s = \text{Sample/sec} = \frac{1}{2} \text{ Sample/sec.}$$



$$x(t) = e^{-2t} u(t)$$

Let $T_s = 1 \text{ Sec}$

$$t = n \cdot T_s$$

$$x[n] = e^{-2n} u[n]$$

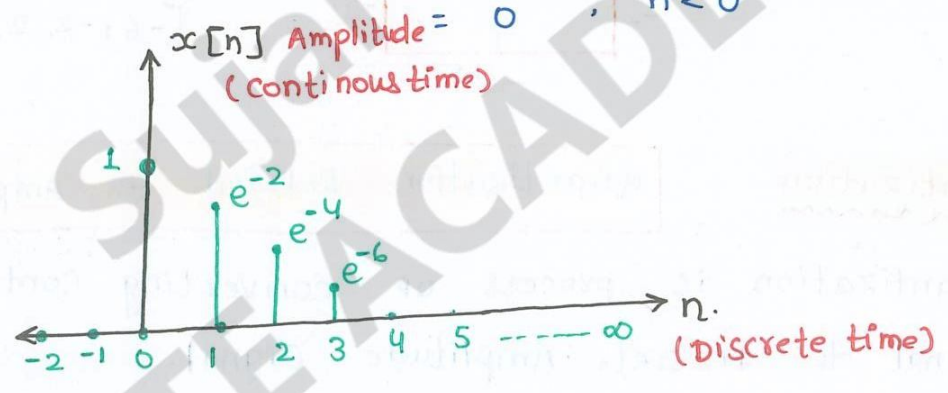
$$x(n \cdot T_s) = e^{-2(n \cdot T_s)} \cdot u[n \cdot T_s]$$

where, n :- Integer only.

(2) Discrete time & Continuous Amplitude Signal

$$x[n] = e^{-2n} \cdot u[n] = e^{-2n} \cdot 1, n \geq 0$$

$$\text{Amplitude} = 0, n < 0$$



(No. of Sample) $n : 0 \rightarrow \infty$
 Amplitude = $1 \rightarrow 0$

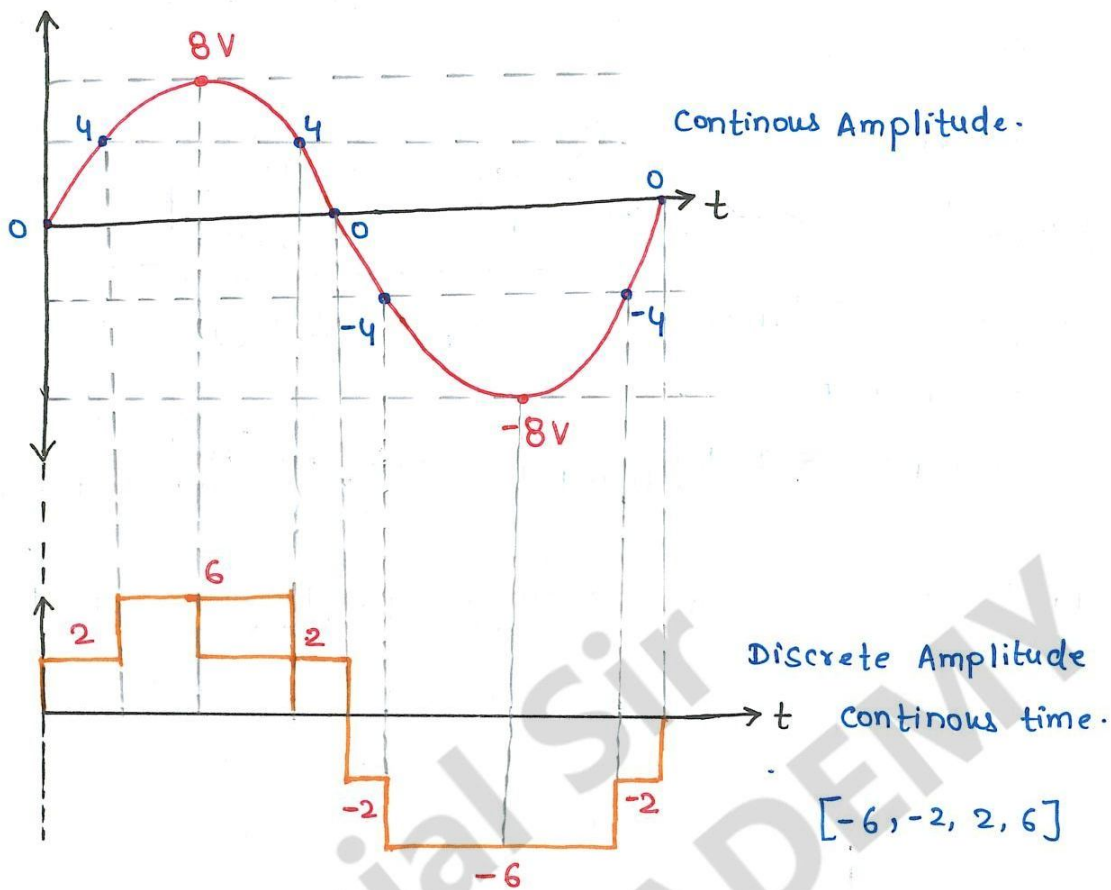
CT $\xrightarrow{\text{Convert}}$ DT

Sampling related to time.

Note :-

- Sampling is the process of converting continuous time signal into discrete time signal.

(3) Discrete Amplitude & Continuous time signal

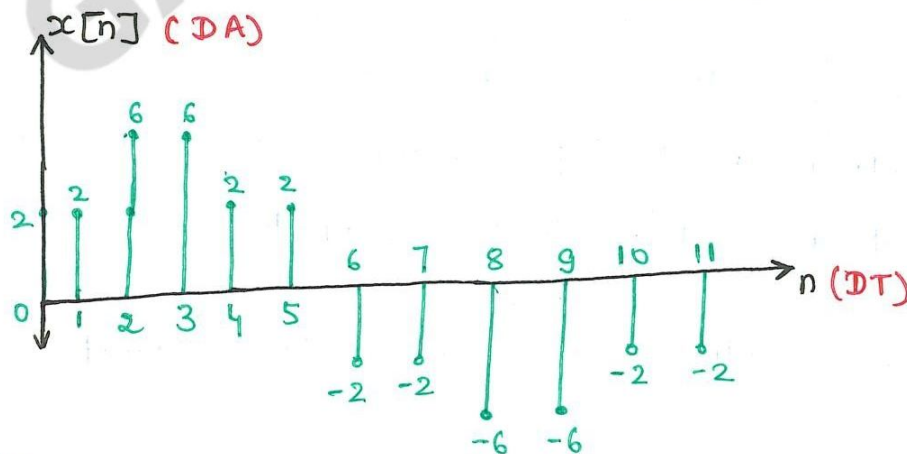


Quantization

Quantization Related to Amplitude.

- Quantization is process of converting Continuous Amplitude signal to Discrete Amplitude signal.

(4) Discrete time & Discrete Amplitude signal



Continuous Amplitude \rightarrow Analog Signal
Discrete Amplitude \rightarrow Digital Signal

- IF signal Nature is Analog or digital depends upon Nature of Amplitude of Any signal.

*** In Above four classification:-

- (i) CT & CA \rightarrow Analog signal
- (ii) DT & CA \rightarrow Analog signal
- (iii) DA & CT \rightarrow Digital signal
- (iv) DA & DT \rightarrow Digital signal.

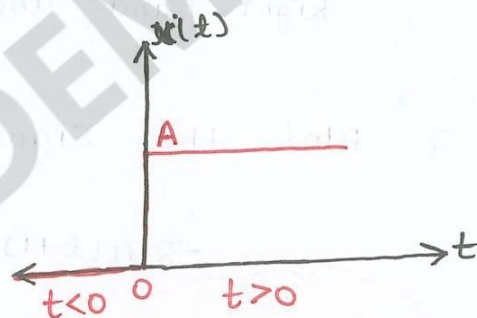
By default
Discrete \rightarrow DT
Continuous \rightarrow CT

Standard Elementary Signals :-

(1) Step Signal

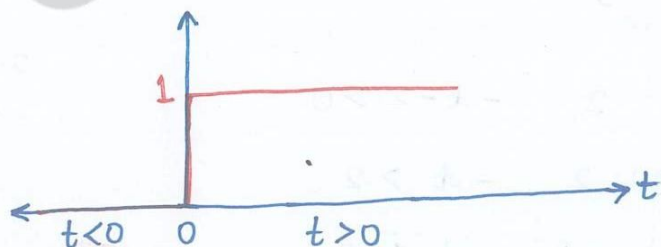
$$x(t) = A \cdot u(t) = A \quad t > 0$$

$$A \cdot u(t) = 0 \quad t < 0$$



Note :-

- At $t=0$ (sudden change in Amplitude (discontinuity) that's why signal Amplitude is not defined at $t=0$.
- IF $A=1$ (unit step signal).



$$x(t) = u(t) = 1 \quad t > 0$$

$$0 \quad t < 0$$

Q. Plot the signal.

$$x(t) = 2 \cdot u(t-2)$$

$$2 \cdot u(t-2) = 2, \quad t-2 > 0$$

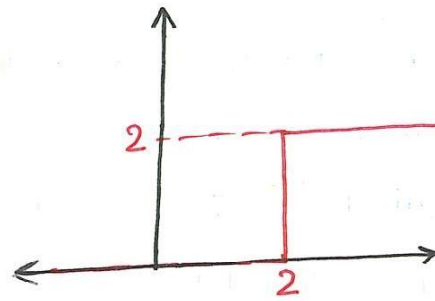
$$= 0, \quad t-2 < 0$$

Change all (t) to (t-2).

$$2 \cdot u(t-2) = 2, \quad t > 2$$

$$0, \quad t < 2$$

Delayed \rightarrow Right Hand.



Key:-

any signal (t-2) sign is Negative then signal shifted to Right hand and delayed signal with time.

Q. Plot the signal. $x_2(t) = -3 \cdot u(t+1)$

$$-3 \cdot u(t+1) = -3, \quad t+1 > 0$$

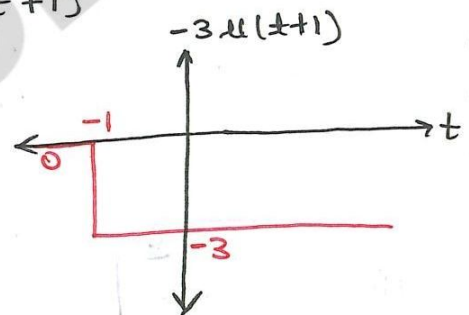
$$= -3, \quad t > -1$$

$$= 0, \quad t < -1$$

Advance \rightarrow Left hand

Key:-

any signal is time added with any value then signal shifted to Left hand side and signal Advance with time.



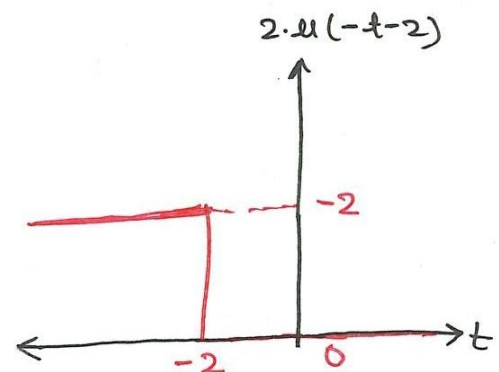
Q. $x_3(t) = 2 \cdot u(-t-2)$

$$2 \cdot u(-t-2) = 2, \quad -t-2 > 0$$

$$= 2, \quad -t > 2$$

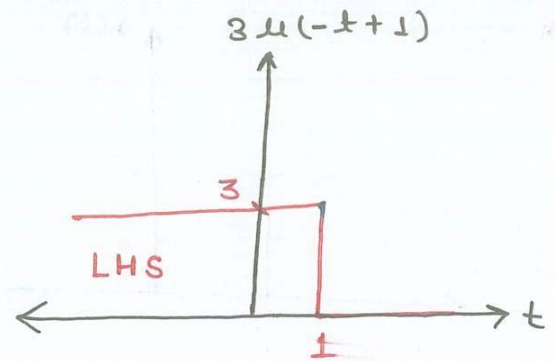
$$= 2, \quad t < -2$$

$$= 0, \quad t > 0$$



Q. Draw $x(t) = 3 \cdot u(-t+1)$

$$\begin{aligned} 3 u(-t+1) &= 3 & -t+1 > 0 \\ &= 3 & -t > -1 \\ &= 3 & t < 1 \\ &= 0 & t > 1 \end{aligned}$$

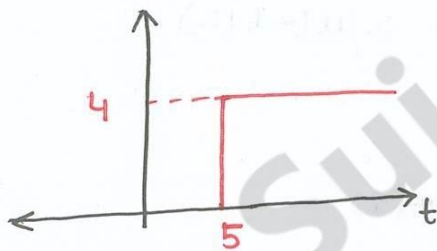


key point :-

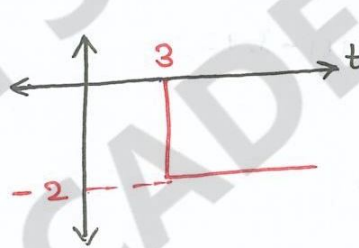
V.V.I

- If t sign is negative then signal is left sided but constant term is same as started ^{move.} point.
 - If t sign is positive then signal is right sided but constant term is reversed. ^{move.}

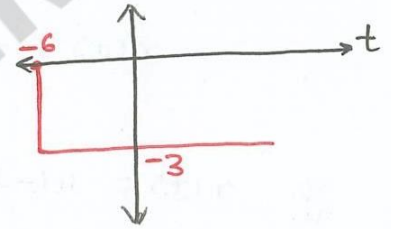
Q. $x(t) = 4 \cdot u(t-5)$



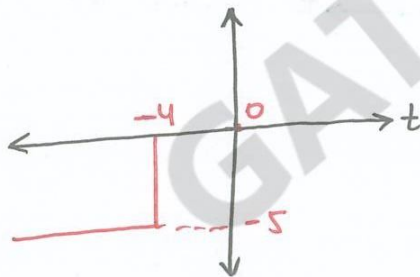
Q. $x(t) = -2 \cdot u(t-3)$



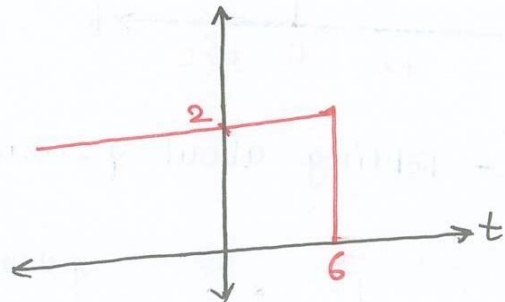
Q. $x(t) = -3 u(t+6)$



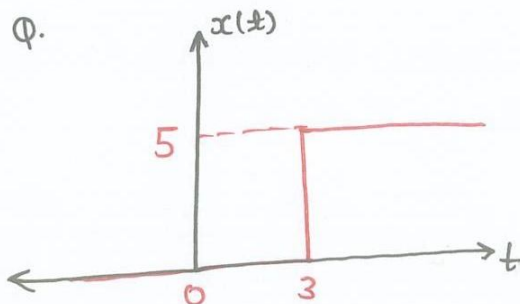
Q. $x(t) = -5 u(-t-4)$



Q. $x(t) = 2 \cdot u(-t+6)$



Q.

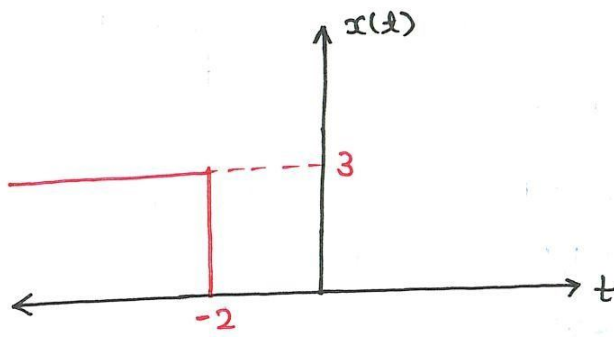


$$x(t) = 5 \cdot u(t-3)$$

$$\begin{aligned} x(t) &= 5, t > 3 & u(t) &= 1, t > 0 \\ &= 5, t-3 > 0 & &= 0, t < 0 \\ &= 0, t-3 < 0 & & \end{aligned}$$

$$x(t) = 5 u(t-3)$$

Q.

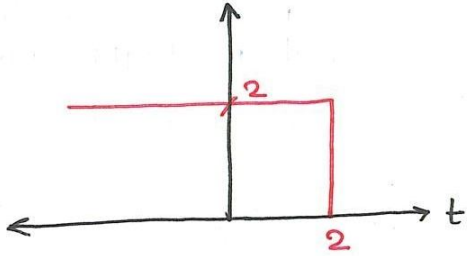


$$x(t) = 3 \cdot u(-t-2)$$

$$\begin{aligned} x(t) &= 3, t < -2 \\ &= 3, -t-2 > 0 \\ &= 0, -t-2 < 0 \end{aligned}$$

$$x(t) = 3 \cdot u(-t-2)$$

Q.



$$x(t) = 2 u(-t+2)$$

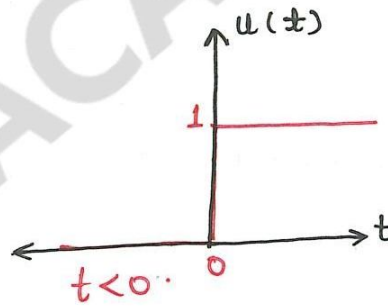
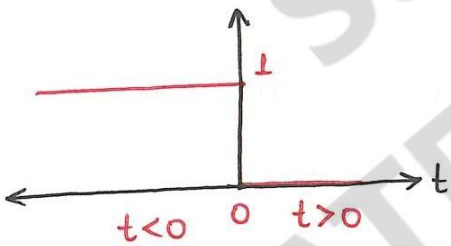
$$x(t) = 2 \quad t < 2$$

$$= 2, -t+2 > 0$$

$$= 0, -t+2 < 0$$

$$x(t) = 2 u(-t+2)$$

Q. $x(t) = u(-t)$



- Folding about y-axis.

